# Particle Swarm Optimization

An introduction and its recent developments

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## Outline

- Swarm Intelligence
- n Introduction to PSO
  - $_{\rm q}~$  PSO real-world applications
  - g PSO variants
  - $_{\mbox{\tiny q}}$  Communication topologies
- n Speciation and niching methods in PSO
- <sup>n</sup> PSO for optimization in dynamic environments
- n PSO for multiobjective optimization





# Swarm Intelligence

## Mind is social...

Human intelligence results from social interaction: Evaluating, comparing, and imitating one another, learning from experience and emulating the successful behaviours of others, people are able to adapt to complex environments through the discovery of relatively optimal patterns of attitudes, beliefs, and behaviours. (Kennedy & Eberhart, 2001).

Culture and cognition are inseparable consequences of human sociality: Culture emerges as individuals become more similar through mutual social learning. The sweep of culture moves individuals toward more adaptive patterns of thought and behaviour.



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Swarm Intelligence applications
Swarm-bots, an EU project led by Marco Dorigo, aimed to study new approaches to
the design and implementation of self-organizing and self-assembling artifacts
(http://www.swarm-bots.org).
A 1992 paper by M. Anthony Lewis and George A. Bekey discusses the possibility of
using swarm intelligence to control **nanobots** within the body for the purpose of killing
cancer tumors.
A Artists are using swarm technology
as a means of creating complex

as a means of creating complex interactive environments. - Disney's *The Lion King* was the first movie to make use of swarm technology (the stampede of the bisons scene). - The movie "*Lord of the Rings*" has also made use of similar technology during battle scenes.



(Some examples from Wikipedia)

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# Novel about swarm



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"... Within hours of his arrival at the remote testing center, Jack discovers his wife's firm has created selfreplicating nanotechnology--a literal swarm of microscopic machines. Originally meant to serve as a military eye in the sky, the swarm has now escaped into the environment and is seemingly intent on killing the scientists trapped in the facility." (Michael Crichton, 2002)



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Particle Swarm Optimization
 Pso has its roots in Artificial Life and social psychology, as well as engineering and computer science.
 The particle swarms in some way are closely related to cellular automata (CA).
 a individual cell updates are done in parallel
 ach new cell value depends only on the old values of the cell and its neighbours, and
 all cells are updated using the same rules (Rucker, 1999).
 Individuals in a particle swarm can be conceptualized as cells in a CA, stose states change in many dimensions simultaneously.

Particle Swarm Optimization As described by the inventers James Kennedy and Russell Eberhart, "particle swarm algorithm imitates human (or insects) social behavior. Individuals interact with one 53 another while learning from their own experience, and gradually the population 43 5 members move into better regions of the problem space". 63 57 4-----23 Why named as "Particle", not "points"? Both Kennedy and Eberhart felt that velocities and accelerations are more appropriately applied to particles. 11 4/10/200



## **PSO** Precursors

Reynolds (1987)'s simulation  $\frac{\text{Boids}}{\text{Boids}}$  – a simple flocking model consists of three simple local rules:

- Collision avoidance: pull away before they crash into one another;
- Velocity matching: try to go about the same speed as their neighbours in the flock;
- Flock centering: try to move toward the center of the flock as they perceive it.

A demo: <u>http://www.red3d.com/cwr/boids/</u> With just the above 3 rules, **Boids** show very realistic flocking behaviour.

Heppner (1990) interests in rules that enabled large numbers of birds to flock synchronously.

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# PSO applications Problems with continuous, discrete, or mixed search space, with multiple local minima. Evolving neural networks: Human tumor analysis; Computer numerically controlled milling optimization; Battery pack state-of-charge estimation; Real-time training of neural networks (Diabetes among Pima Indians); Seroomechanism (time series prediction optimizing a neural network); Reactive power and voltage control; Ingredient mix optimization; Pressure vessel (design a container of compressed air, with many constraints);

- S Compression spring (cylindrical compression spring with certain machanical characteristica):
- mechanical characteristics);
   Moving Peaks (multiple peaks dynamic environment); and more

PSO can be tailor-designed to deal with specific real-world problems.

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Fully Informed PSO (FIPS) The two terms in the constriction PSO are of the same form, hence can be condensed to the following (Mendes & Kennedy, 2004):  $\vec{v}_{t+1} = \chi(\vec{v}_t + \vec{\phi}_m \otimes (\vec{p}_m - \vec{x}_t))$   $\vec{x}_{t+1} = \vec{x}_t + \vec{v}_{t+1}$ Where  $\vec{\phi}_m = \vec{\phi}_t + \vec{\phi}_2$  and  $\vec{p}_m = (\vec{\phi}_t \otimes \vec{p}_t + \vec{\phi}_2 \otimes \vec{p}_s)/(\vec{\phi}_t + \vec{\phi}_2)$ . This shows that that a particle tends to converge towards a point determined by  $\vec{p}_m$ , which a weighted average of its previous best  $\vec{p}_i$  and the neighbourhood's best  $\vec{p}_s$ .  $\vec{F}_m$  can be further generalized to any number of terms.  $\vec{v}_{t+1} = \chi(\vec{v}_t + \sum_{k \in N} \vec{R}[0, \frac{\theta}{|N|}] \otimes (\vec{p}_k - \vec{x}_t))$ . Motenotes the neighbourhood, and  $\vec{p}_i$  the best previous position found by the *k*-th particle in *N*. If |*N*| equals 2, then the above is a generalization of the canonical PSO.







## Some PSO variants

- S Tribes (Clerc, 2006) aims to adapt population size, so that it does not have to be set by the users;
- ARPSO (Riget and Vesterstorm, 2002) uses a diversity measure to alternate between 2 phases;
- S Dissipative PSO (Xie, et al., 2002) increasing randomness;
- PSO with self-organized criticality (Lovbjerg and Krink, 2002) aims to improve diversity;
- § Self-organizing Hierachicl PSO (Ratnaweera, et al. 2004);
- § FDR-PSO (Veeramachaneni, et al., 2003) using nearest neighbour interactions;
- § PSO with mutation (Higashi and Iba, 2003; Stacey, et al., 2004)
- $\,{\mathbb S}\,$  Cooperative PSO (van den Bergh and Engelbrecht, 2005) a cooperative approach
- DEPSO (Zhang and Xie, 2003) aims to combine DE with PSO;
- S CLPSO (Liang, et al., 2006) incorporate learning from more previous best particles.

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# Communication topologies (4)

## Which one to use?

Balance between exploration and exploitation...

gbest model propagate information the fastest in the population; while the lbest model using a ring structure the slowest. For complex multimodal functions, propagating information the fastest might not be desirable. However, if this is too slow, then it might incur higher computational cost.

Mendes and Kennedy (2002) found that von Neumann topology (north, south, east and west, of each particle placed on a 2 dimensional lattice) seems to be an overall winner among many different communication topologies.

Speciation and niching

## Speciation and niching

Biological species concept: a species is a group of actually or potentially interbreeding individuals who are reproductively isolated from other such groups.

The definition of a species is still debatable

Most researchers believe either the morphological species concept (ie., members of a species look alike and can be distinguished from other species by their appearance), or the **biological** species concept (a species is a group of actually) or potentially interbreeding individuals who are reproductively isolated from other such groups). Both definitions have their weaknesses.

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## Speciation and niching

- Kennedy (2000) proposed a *k*-means clustering technique; Parsopoulos and Vrahitis (2001) used a stretching function; Brits et al. (2002) proposed a NichePSO; Many other niching methods developed for Evolutionary Algorithms, such as S S
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- owding metho fitness-sharing, cle aring, etc.
- Petrowski (1996) introduced a clearing procedure, and later on Li, et al. (2002) introduced a species conserving genetic algorithm (SCGA) for multimodal optimization.

## The notion of species:

- S A population is classified into groups according to their similarity measured by Euclidean distance.
- ${\rm S}~$  The definition of a species also depends on another parameter  $r_{\!s}$  ,which denotes the radius measured in Euclidean distance from the center of the a species to its boundary.

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# Speciation-based PSO

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# Multimodal problems















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# Test functions for dynamic optimization

Juergen Branke's **Moving peak test functions** - The moving peak benchmark (MPB) is widely used in the EC community. A few recent PSO works also adopted it (Clerc, 2006; Blackwell and Branke, 2004; Li et al., 2006). For more information, refer to:

http://www.aifb.uni-karlsruhe.de/~jbr/MovPeaks/

Morrison and De Jong's **DF1** function generator – one of the early dynamic test function generator proposed (Morrison, 2005). A few authors have used it (Parrott and Li, 2006).

A few other dynamic test functions have also been proposed in recent years.

A demonstration run of SPSO tracking the global peak in a 10 peaks dynamic environment (Moving peaks Scienario2). Refer to (Li, et al. 2006) for details.

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# NSPSO Algorithm

## The basic idea:

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- Instead of comparing solely on a particle's personal best with its potential offspring, the entire population of N particles' personal bests and N of these particles' offspring are first combined to form a temporary population of 2N particles. After this, domination comparisons among all the 2N individuals in this temporary population are carried out.
- S Sort the entire population in different non-domination levels (as in NSGA II). This type of sorting can then be used to introduce the selection bias to the individuals in the populations, in favour of individuals closer to the true Pareto front.
- S At each iteration step, we choose only N individuals out of the 2N to the next iteration step, based on the non-domination levels, and two niching methods.

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